# Use of equations for the description of experimental dependence of the height equivalent to a theoretical plate on carrier gas velocity in capillary gas-liquid chromatography 

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#### Abstract

Optimal equation for fitting the experimental data on the height equivalent to a theoretical plate (HETP) versus carrier gas velocity in GLC was determined. The data obtained by authors and the literary data by other investigators were used for the comparative study of Van Deemter, Golay and the little known Golay-Guiochon equations. The Golay-Guiochon equation takes into account instrumental contribution and other sources of additional band broadening. Correlation coefficient $R$ and Pirson's criterion $\chi^{2}$ were used as a criterion of the data correspondence to the equations. The Golay-Guiochon equation is the best for fitting of the experimental data in $71 \%$ considered examples, $19 \%$ experimental data may be fitted very precisely by the Van Deemter equation, the Golay equation is preferable for $7 \%$ experimental data only. Three percent experimental data may be fitted with the same precision by the Golay and the Van Deemter equations. The results obtained are of theoretical and practical interest. The Golay-Guiochon equation must be used more widely in analytical practice and physicochemical measurements. © 2000 Elsevier Science B.V. All rights reserved.


Keywords: Band broadening; Height equivalent to a theoretical plate; Flow velocity

## 1. Introduction

The phenomenon of Band broadening in a chromatographic column is very complex. It is of great importance for analytical purposes because zones' broadening leads to falling off in separation. Hence, the phenomenon is widely covered in the literature (see, e.g., Refs. [1-5]).

Note that the determination of the optimal dependence (in reference to the experimental data) of height equivalent to a theoretical plate (HETP, $H$ ) on

[^0]the carrier gas velocity $(u)$ is a necessary and an important stage when studying the nature of the band broadening, interpreting the phenomenon, optimising the separation:
\[

$$
\begin{equation*}
H=f(u) \tag{1}
\end{equation*}
$$

\]

In the modern scientific literature the Van Deemter equation for packed columns [6] and the Golay equation for capillary columns [7-9] are in common use. These remarkable equations published more than 40 years ago were the first to allow chromatographers to offer correct physicochemical explana-
tion of the band broadening and to propose the fundamentals for separation optimisation. The equations are of great importance now.

In our opinion, the Golay-Guiochon [10] equation is promising. Unlike the Van Deemter and the Golay equations, the Golay-Guiochon equation takes into account extra-column band broadening (for example, the instrumental contributions). This equation is little known and discussed in some studies by Guiochon and co-workers [10-12].

It should be noted that, although the Van Deemter equation was proposed for packed columns only, we used it in the given study according to Desty and Goldup who applied the equation to capillary gasliquid columns [13].

Let us consider the above-mentioned equations.
In the well-known studies by Golay [7-9] the band broadening due to the longitudinal diffusion in carrier gas flow and final rate of mass transfer in gas and liquid phases was considered. Golay's equation can be presented in the simple form as:
$H=B_{1} / u+C_{1} u$
where
$B_{1}=2 D_{\mathrm{g}}$
$C_{1}=C_{\mathrm{G}}+C_{\mathrm{L}}$
$C_{\mathrm{G}}=\frac{1+6 k+11 k^{2}}{24(1+k)^{2}} \cdot \frac{r^{2}}{D_{\mathrm{G}}}$
$C_{\mathrm{L}}=\frac{2 k}{3(1+k)^{2}} \cdot \frac{d_{\mathrm{f}}^{2}}{D_{\mathrm{L}}}$
where $D_{\mathrm{G}}$ is the diffusion coefficient in the gas phase, $k$ is the retention factor, $r$ is the radius of capillary column, $d_{\mathrm{f}}$ is the film thickness of stationary liquid phase (SLP) in the column, $D_{\mathrm{L}}$ is the diffusion coefficient in SLP, $B_{1}$ is the longitudinal diffusion term, $C_{\mathrm{G}}$ and $C_{\mathrm{L}}$ are the coefficients of the resistance to mass transfer in the mobile and stationary phases, respectively.

The Golay equation bases on the distinct physical model of the band broadening and the observed regularities of the band broadening on the experimental parameters may be fitted very precisely by the equation. Unfortunately, only limited publications on this matter are available (see, e.g., Refs.
$[14,15])$ and this problem in capillary GLC does not appear to be discussed in the most excellent monographs [1-5].

In 1978 Guiochon and co-workers proposed the equation taking into account the extra-column band broadening. We take this equation as the GolayGuiochon equation.
$H=B_{2} / u+C_{2} u+D_{\text {ex }} u^{2}$
where
$B_{2}=2 D_{\mathrm{g}}$
$C_{2}=\frac{1+6 k+11 k^{2}}{24(1+k)^{2}} \cdot \frac{r_{0}^{2}}{D_{\mathrm{g}}}+\frac{2 k}{3(1+k)^{2}} \cdot \frac{d_{\mathrm{f}}^{2}}{D_{\ell}}$
$D_{\mathrm{ex}}=\frac{\sigma_{\mathrm{t}}^{2}}{(1+k)^{2} L}$
where $D_{\mathrm{g}}$ is the diffusion coefficient in the gas phase, $k$ is the retention factor, $r_{0}$ is the radius of capillary, $d_{\mathrm{f}}$ is the film thickness of SLP, $D_{1}$ is the diffusion coefficient in SLP, $\sigma_{t}^{2}$ is the dispersion characterizing the extra-column band broadening, $L$ is the column length, $D_{\text {ex }}$ is the main characteristic of the extra-column band broadening in Eq. (7) ( $D_{\text {ex }} u^{2}$ is the extra-column band broadening expressed in $H$ values.)

Unfortunately, there are only limited publications (see, e.g., Refs.[10-12]) where Eq. (7) was used in capillary GLC for the fitting the experimental data and the determination of $B_{2}, C_{2}$ and $D_{\text {ec }}$ coefficients. But the Golay-Guiochon equation is very promising since the extra-column band broadening usually takes place at real experimental conditions, especially under high-speed conditions.

According to Guiochon and co-workers [10], who suggested introducing the additional term $D_{\text {ex }} u^{2}$ into the Golay's equation, this term is a result of time constants of the electronic components registering the chromatographic zones. But, it should be noted that the nature of the processes contributed to the extra-column band broadening is wider. It seems likely that the contribution of the band broadening due to the final width of the initial zone before the column is also of great importance along with the 'electronic reason'.

The equation proposed by Van Deemter et al. [6] can be given as follows:

Table 1
Characteristics of chromatographic systems used for the calculations

|  | Column | SLP | Carrier |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| gas |  |  |  |

Table 1 (continued)

|  | Column | SLP | Carrier <br> gas | Sorbate | $T\left({ }^{\circ} \mathrm{C}\right)$ | Ref. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L1 | $25 \mathrm{~m} \times 0.16 \mathrm{~mm}$ | $\begin{aligned} & \text { SE-30 } \\ & \left(d_{\mathrm{f}}=0.25 \mu \mathrm{~m}\right) \end{aligned}$ | $\mathrm{N}_{2} \mathrm{O}$ | Naphthalene | 130 | A |
| M1 | $85 \mathrm{~cm} \times 65 \mu \mathrm{~m}$ | Squalane | $\mathrm{H}_{2}$ | $n$-Heptane | 20 | [10] |
| M2 |  |  | $\mathrm{H}_{2}$ | $n$-Octane | 20 |  |
| M3 | $100 \mathrm{~cm} \times 65 \mu \mathrm{~m}$ | - | $\mathrm{H}_{2}$ | Methane | 20 |  |
| M4 |  |  | $\mathrm{H}_{2}$ | $n$-Hexane | 20 |  |
| M5 |  |  | $\mathrm{N}_{2}$ | Methane | 20 |  |
| M6 |  |  | $\mathrm{N}_{2}$ | $n$-Hexane | 20 |  |
| N1 | $30 \mathrm{~m} \times 0.32 \mathrm{~mm}$ | $\begin{aligned} & \text { SPB-1 } \\ & \left(d_{\mathrm{f}}=0.25 \mu \mathrm{~m}\right) \\ & \text { WAX-10 } \end{aligned}$ | He | Naphthalene | 160 | [17] |
| N2 | - | $\left(d_{\mathrm{f}}=0.25 \mu \mathrm{~m}\right)$ | He | Naphthalene | 160 |  |
| O1 | $20 \mathrm{~m} \times 0.27 \mathrm{~mm}$ | Dimethyl | $\mathrm{N}_{2}$ | $n$-Tridecane | 100 | [15] |
| O2 |  | siloxane | He | $n$-Tridecane |  |  |
| O3 |  | ( $d_{\mathrm{f}}=0.22 \mu \mathrm{~m}$ ) | $\mathrm{H}_{2}$ | $n$-Tridecane |  |  |
| P1 | $37 \mathrm{~m} \times 0.18 \mathrm{~mm}$ | Dimethyl | $\mathrm{H}_{2}$ |  | 100 | [15] |
| P2 | $60 \mathrm{~m} \times 0.27 \mathrm{~mm}$ | siloxane | $\mathrm{H}_{2}$ | $n$-Dodecane | 100 |  |
| P3 | $58 \mathrm{~m} \times 0.51 \mathrm{~mm}$ |  | $\mathrm{H}_{2}$ | $n$-Dodecane | 100 |  |
| P4 | $50 \mathrm{~m} \times 0.70 \mathrm{~mm}$ |  | $\mathrm{H}_{2}$ | $n$-Dodecane | 100 |  |
| P5 | $49 \mathrm{~m} \times 0.88 \mathrm{~mm}$ |  | $\mathrm{H}_{2}$ | $n$-Dodecane | 100 |  |
| Q1 | $25 \mathrm{~m} \times 0.32 \mathrm{~mm}$ | Dimethyl siloxane $\left(d_{\mathrm{f}}=3 \mu \mathrm{~m}\right)$ | $\mathrm{H}_{2}$ | Compound with $k=10$ | 85 | [15] |
| Q2 | $25 \mathrm{~m} \times 0.53 \mathrm{~mm}$ | As Q1 | $\mathrm{H}_{2}$ | Compound with $k=10$ |  |  |
| Q3 | $25 \mathrm{~m} \times 0.32 \mathrm{~mm}$ | Diphenyl dimethyl siloxane ( $\left.d_{\mathrm{f}}=3 \mu \mathrm{~m}\right)$ | $\mathrm{H}_{2}$ | Compound with $k=10$ |  |  |
| Q4 | $25 \mathrm{~m} \times 0.53 \mathrm{~mm}$ | As Q3 | $\mathrm{H}_{2}$ | Compound with $k=10$ |  |  |
| R1 | $3 \mathrm{~m} \times 0.15 \mathrm{~mm}$ | $\begin{aligned} & \text { CP-Sil 5CB } \\ & \left(d_{\mathrm{f}}=0.12 \mu \mathrm{~m}\right) \end{aligned}$ | $\mathrm{H}_{2}$ | $n$-Octane | 40 | [11] |
| R2 | $3.8 \mathrm{~m} \times 0.15 \mathrm{~mm}$ | As R1 | $\mathrm{H}_{2}$ | $n$-Octane |  |  |
| S1 | $25 \mathrm{~m} \times 0.53 \mathrm{~mm}$ | 5-Phenyl95\%methyl polysiloxane ( $d_{\mathrm{f}}=3 \mu \mathrm{~m}$ ) | - | $n$-Dodecane | 125 | [4] |
| T1 | $25 \mathrm{~m} \times 0.25 \mathrm{~mm}$ | OV-1 | $\mathrm{H}_{2}$ | $n$-Heptadecane | 175 | [2] |
| T2 |  | $\left(d_{\mathrm{f}}=0.4 \mu \mathrm{~m}\right)$ | He |  |  |  |
| T3 |  |  | $\mathrm{N}_{2}$ |  |  |  |

${ }^{\text {a }}$ Authors experimental data.
$H=A+B_{3} / u+C_{3} u$
where $A$ is the eddy diffusion term, $B_{3}$ is the longitudinal diffusion term, $C_{3}$ is the coefficient of resistance to mass transfer. All the constants of the equations used in the present study were determined
using experimental values $(H, u)$ for the given dependence. A criterion is a minimisation of standard deviation value of HETP for all experimental data $\operatorname{HETP}=f(u)$ fitted by the given equation.
Note, each equation from those considered above reflects an individual physicochemical concept. The

Table 2
Results of calculation for various equations

|  | $H=A+B_{3} / u+C_{3} u(11)$ |  |  |  | $H=B_{1} / u+C_{1} u(2)$ |  |  | $H=B_{2} / u+C_{2} u+D_{\text {ex }}^{2}(7)$ |  |  |  | Optimal equation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $A(\mathrm{~cm})$ | $\begin{aligned} & B_{3} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{3}(\mathrm{~s})$ | $\chi^{2}\left(\times 10^{6}\right)$ | $\begin{aligned} & B_{1} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{1}(\mathrm{~s})$ | $\chi^{2}$ | $\begin{aligned} & B_{2} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{2} \times 10^{4}$ <br> (s) | $D_{\text {ex }} \times 10^{6}$ | $\chi^{2}$ |  |
| A1 | -0.106 | 0.428 | 0.0071 | 6.02 | 0.019 | 0.0042 | 16.96 | 0.153 | -10.0 | 13.80 | 0.60 | 7 |
| A2 | $-0.022$ | 0.129 | 0.0030 | 0.80 | 0.043 | 0.0024 | 6.00 | 0.065 | 15.0 | 2.34 | 1.50 | 11 |
| A3 | $-0.031$ | 0.182 | 0.0038 | 1.40 | 0.069 | 0.0027 | 9.40 | 0.096 | 15.0 | 4.25 | 4.40 | 11 |
| A4 | -0.043 | 0.200 | 0.0047 | 5.40 | 0.034 | 0.0036 | 24.10 | 0.070 | 22.0 | 3.70 | 14.80 | 11 |
| A5 | -0.034 | 0.248 | 0.0038 | 5.30 | 0.120 | 0.0.29 | 17.00 | 0.145 | 17.0 | 3.12 | 10.30 | 11 |
| A6 | -0.012 | 0.219 | 0.0026 | 0.60 | 0.171 | 0.0022 | 1.90 | 0.185 | 18.0 | 1.25 | 0.70 | 11 |
| A7 | -0.040 | 0.196 | 0.0035 | 15.50 | 0.042 | 0.0024 | 29.90 | 0.095 | 3.0 | 5.48 | 5.00 | 7 |
| A8 | -0.041 | 0.318 | 0.0042 | 6.90 | 0.170 | 0.0028 | 19.40 | 0.218 | 7.0 | 7.28 | 2.80 | 7 |
| A9 | -0.021 | 0.160 | 0.0026 | 11.40 | 0.079 | 0.0021 | 14.20 | 0.111 | 8.0 | 3.24 | 6.20 | 7 |
| A10 | -0.016 | 0.148 | 0.0026 | 1.10 | 0.086 | 0.0021 | 3.60 | 0.104 | 14.0 | 1.86 | 0.80 | 7 |
| A11 | -0.141 | 0.1020 | 0.0070 | 1.50 | 0.055 | 0.0038 | 7.91 | 0.355 | -3.0 | 10.10 | 10.00 | 11 |
| B1 | -0.057 | 1.040 | 0.0024 | 1.10 | 0.400 | 0.0015 | 0.78 | 0.581 | 5.0 | 1.77 | 0.09 | 7 |
| B2 | $-0.035$ | 0.815 | 0.0017 | 0.30 | 0.421 | 0.0012 | 0.28 | 0.530 | 6.0 | 1.04 | 0.40 | 11 |
| C1 | -0.029 | 0.715 | 0.0013 | 0.20 | 0.369 | 0.0008 | 0.11 | 0.486 | 2.0 | 1.19 | 0.02 | 7 |
| D1 | $-0.073$ | 1.420 | 0.0021 | 0.50 | 0.811 | 0.0009 | 1.51 | 0.997 | $-10.0$ | 4.13 | 0.23 | 7 |
|  | -0.055 | 1.152 | 0.0028 | 12.00 | 0.803 | 0.0014 | 16.80 | 0.926 | -5.0 | 5.54 | 7.00 | 7 |
| F1 | -0.057 | 1.320 | 0.0014 | 0.10 | 0.779 | 0.0003 | 0.68 | 0.964 | $-11.0$ | 3.08 | 0.05 | 7 |
| G1 | -0.070 | 1.111 | 0.0030 | 0.30 | 0.681 | 0.0010 | 1.17 | 0.810 | $-13.0$ | 7.54 | 0.17 | 7 |
| G2 | $-0.061$ | 0.927 | 0.0034 | 4.30 | 0.550 | 0.0016 | 12.10 | 0.673 | -5.0 | 6.79 | 4.00 | 7 |
| H1 | $-0.024$ | 0.502 | 0.0021 | 3.30 | 0.360 | 0.0014 | 4.30 | 0.422 | 2.0 | 4.19 | 2.10 | 7 |
| H2 | -0.011 | 0.585 | 0.0003 | 2.60 | 0.649 | 0.0059 | 2.30 | 0.645 | 7.0 | 0.28 | 2.90 | 2 |
| H3 | $-0.027$ | 0.720 | 0.0017 | 1.30 | 0.561 | 0.0009 | 2.60 | 0.610 | 0 | 3.30 | 1.20 | 7 |
| H4 | -0.019 | 0.795 | 0.0019 | 2.30 | 0.680 | 0.0014 | 2.60 | 0.721 | 6.0 | 2.65 | 1.90 | 7 |
| I1 | $-0.052$ | 1.029 | 0.0010 | 0.60 | -0.074 | 0.0006 | 0.63 | 0.277 | 0.6 | 0.50 | 0.20 | 7 |
| I2 | -0.052 | 1.130 | 0.0011 | 0.20 | 0.011 | 0.0007 | 0.60 | 0.349 | 1.6 | 0.48 | 0.05 | 7 |
| I3 | $-0.057$ | 1.241 | 0.0010 | 0.40 | 0.019 | 0.0006 | 0.73 | 0.402 | 0.4 | 0.55 | 0.20 | 7 |
| I4 | -0.072 | 1.311 | 0.0014 | 0.70 | -0.231 | 0.0008 | 1.19 | 0.258 | 0.7 | 0.70 | 0.20 | 7 |
| I5 | -0.065 | 1.348 | 0.0012 | 0.50 | -0.029 | 0.0007 | 0.95 | 0.409 | 0.5 | 0.62 | 0.10 | 7 |
| I6 | -0.069 | 1.430 | 0.0012 | 1.00 | -0.038 | 0.0007 | 1.11 | 0.438 | 1.0 | 0.68 | 0.01 | 7 |
| I7 | -0.099 | 1.742 | 0.0019 | 2.90 | -0.382 | 0.0010 | 2.38 | 0.316 | 2.9 | 0.99 | 0.40 | 7 |
| J1 | -0.093 | 0.621 | 0.0041 | 3.80 | $-0.200$ | 0.0025 | 4.00 | 0.059 | 3.0 | 3.98 | 0.70 | 7 |
| J2 | -0.109 | 0.737 | 0.0049 | 5.50 | -0.221 | 0.0029 | 5.54 | 0.078 | 3.0 | 4.69 | 0.90 | 7 |
| J3 | -0.099 | 0.676 | 0.0044 | 6.20 | -0.199 | 0.0026 | 4.75 | 0.079 | 2.0 | 4.33 | 0.11 | 7 |
| J4 | -0.110 | 0.688 | 0.0052 | 3.20 | -0.283 | 0.0033 | 5.37 | 0.090 | 8.0 | 4.46 | 0.47 | 7 |
| J5 | -0.115 | 0.772 | 0.0051 | 5.80 | -0.241 | 0.0030 | 6.09 | 0.079 | 3.0 | 4.93 | 0.60 | 7 |
| J6 | -0.124 | 0.840 | 0.0054 | 7.80 | -0.250 | 0.0032 | 7.25 | 0.091 | 2.0 | 5.39 | 0.60 | 7 |
| J7 | -0.170 | 1.071 | 0.0074 | 16.40 | -0.419 | 0.0044 | 13.65 | 0.058 | 3.0 | 7.40 | 0.60 | 7 |
| K1 | $-0.070$ | 0.476 | 0.0032 | 2.50 | -0.087 | 0.0020 | 2.24 | 0.075 | 1.8 | 3.30 | 0.30 | 7 |
| K2 | -0.079 | 0.570 | 0.0037 | 5.70 | -0.067 | 0.0023 | 3.08 | 0.124 | 2.4 | 3.89 | 0.20 | 7 |
| K3 | -0.079 | 0.577 | 0.0035 | 5.10 | -0.063 | 0.0021 | 3.50 | 0.127 | 0.4 | 3.91 | 0.30 | 7 |
| K4 | -0.113 | 0.729 | 0.0049 | 7.70 | -0.180 | 0.0032 | 5.98 | 0.083 | 0.8 | 5.42 | 0.80 | 7 |
| K5 | -0.090 | 0.649 | 0.0040 | 5.80 | -0.076 | 0.0024 | 3.86 | 0.138 | 0.5 | 4.40 | 1.00 | 7 |
| K6 | -0.096 | 0.691 | 0.0042 | 7.80 | -0.084 | 0.0025 | 4.51 | 0.147 | 0.8 | 4.71 | 1.00 | 7 |
| K7 | -0.047 | 0.283 | 0.0036 | 9.20 | -0.097 | 0.0028 | 17.30 | 0.098 | 2.1 | 6.30 | 1.00 | 7 |

Table 2 (continued)

|  | $H=A+B_{3} / u+C_{3} u(11)$ |  |  |  | $H=B_{1} / u+C_{1} u(2)$ |  |  | $H=B_{2} / u+C_{2} u+D_{\text {ex }}^{2}(7)$ |  |  |  | Optimal equation |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $A(\mathrm{~cm})$ | $\begin{aligned} & B_{3} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{3}(\mathrm{~s})$ | $\chi^{2}\left(\times 10^{6}\right)$ | $\begin{aligned} & B_{1} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{1}(\mathrm{~s})$ | $\chi^{2}$ | $\begin{aligned} & B_{2} \\ & \left(\mathrm{~cm}^{2} / \mathrm{s}\right) \end{aligned}$ | $C_{2} \times 10^{4}$ <br> (s) | $D_{\text {ex }} \times 10^{6}$ | $\chi^{2}$ |  |
| L1 | $-0.048$ | 0.843 | 0.0023 | 9.50 | 0.570 | 0.0008 | 12.80 | 6.73 | $-13.0$ | 7.70 | 0.69 | 7 |
| M1 | $-0.003$ | 0.634 | 0.0002 | 0.62 | 0.550 | 0.0002 | 5.00 | 0.607 | 1.3 | 0.04 | 0.35 | 7 |
| M2 | -0.009 | 0.729 | 0.0002 | 0.38 | 0.449 | 0.0001 | 2.00 | 0.541 | 0.5 | 0.06 | 3.70 | 7 |
| M3 | -0.071 | 2.490 | 0.0010 | 6.90 | $-0.220$ | 0.0007 | 152.00 | 0.738 | 2.0 | 0.26 | 3.70 | 7 |
| M4 | -0.028 | 1.951 | 0.0002 | 2.90 | 0.573 | 0.0001 | 2.70 | 0.924 | 0.2 | 0.05 | 4.40 | 2 |
| M5 | -0.43 | 1.479 | 0.0006 | 2.80 | -0.170 | 0.0004 | 5.90 | 0.425 | 0.7 | 0.16 | 0.28 | 7 |
| M6 | -0.09 | -0.253 | 0.0001 | 3.40 | 0.182 | 0.0001 | 1.80 | 0.90 | 1.9 | 0.02 | 0.17 | 7 |
| N1 | -0.098 | 2.660 | 0.0018 | 1.00 | 0.860 | 0.0006 | 51.00 | 1.461 | $-7.0$ | 1.85 | 0.40 | 7 |
| N2 | -0.089 | 2.390 | 0.0015 | 0.90 | 0.761 | 0.0005 | 43.00 | 1.319 | -7.0 | 1.71 | 0.30 | 7 |
| 01 | -0.026 | 0.303 | 0.0022 | 2.40 | 0.095 | 0.0018 | 84.00 | 0.164 | 12.0 | 0.88 | 2.00 | 7 |
| O 2 | -0.013 | 0.478 | 0.0008 | 0.09 | 0.239 | 0.0007 | 4.00 | 0.318 | 5.0 | 0.18 | 1.00 | 11 |
| O 3 | -0.017 | 0.956 | 0.0006 | 1.00 | 0.590 | 0.0004 | 5.00 | 0.696 | 3.0 | 0.16 | 2.00 | 11 |
| P1 | $-0.001$ | 0.280 | 0.0004 | 0.50 | 0.260 | 0.0004 | 0.40 | 0.244 | 4.0 | -0.01 | 0.50 | 2 |
| P2 | -0.018 | 0.502 | 0.0009 | 0.30 | 0.064 | 0.0007 | 7.00 | 0.179 | 6.0 | 0.12 | 0.40 | 11 |
| P3 | $-0.013$ | 0.617 | 0.0016 | 4.30 | 0.339 | 0.0014 | 4.30 | 0.377 | 14.0 | 0.05 | 4.90 | 11.2 |
| P4 | -0.002 | 0.417 | 0.0003 | 2.50 | 0.441 | 0.0025 | 2.20 | 0.451 | 25.0 | 0.07 | 2.50 | 2 |
| P5 | -0.010 | 0.548 | 0.0041 | 2.60 | 0.420 | 0.0039 | 2.20 | 0.433 | 38.0 | 0.11 | 2.70 | 2 |
| Q1 | -0.002 | 0.213 | 0.0026 | 0.30 | 0.210 | 0.0026 | 0.30 | 0.208 | 26.0 | -0.01 | 0.40 | 11.2 |
| Q2 | -0.005 | 0.237 | 0.0046 | 0.20 | 0.211 | 0.0045 | 4.00 | 0.221 | 42.0 | 0.67 | 2.00 | 11 |
| Q3 | 0.006 | 0.175 | 0.0137 | 1.00 | 0.190 | 0.0140 | 13.00 | 0.191 | 141.0 | -0.45 | 1.40 | 11 |
| Q4 | 0.014 | 0.173 | 0.0150 | 4.90 | 0.223 | 0.0160 | 50.00 | 0.212 | 161.0 | -2.15 | 53.00 | 11 |
| R1 | $-0.028$ | 0.638 | 0.0008 | 6.70 | 0.351 | 0.0005 | 14.00 | 0.429 | 1.0 | 0.37 | 2.30 | 7 |
| R2 | $-0.022$ | 0.579 | 0.0006 | 2.50 | 0.349 | 0.0005 | 7.80 | 0.427 | 1.0 | 0.25 | 1.10 | 7 |
| S1 | -0.027 | 0.869 | 0.0026 | 24.2 | 0.480 | 0.0024 | 61.00 | 0.595 | 20.0 | 3.28 | 8.16 | 7 |
| T1 | -0.018 | 0.813 | 0.0006 | 0.47 | 0.650 | 0.0003 | 15.50 | 0.690 | -0.3 | 5.99 | 2.68 | 11 |
| T2 | -0.021 | 0.582 | 0.0010 | 3.01 | 0.450 | 0.0006 | 35.10 | 0.479 | 1.8 | 7.36 | 4.07 | 11 |
| T3 | -0.029 | 0.252 | 0.0023 | 5.72 | 0.096 | 0.0017 | 63.90 | 0.136 | 8.4 | 18.8 | 1.63 | 7 |

Golay Eq. (2) takes into account the longitudinal band broadening in the gas phase and the limited rate of mass transfer between the gas and stationary phases. The Golay-Guiochon Eq. (7) additionally takes into account the extra-column band broadening. The Van Deemter Eq. (11) additionally takes into account the band broadening due to the eddy diffusion as compared with the Golay equation.

Thus, the fitting of the experimental data with the Eqs. (2), (7), (9) is simultaneously the checking of the physicochemical concept used for their derivation.

Unfortunately, firstly, the experimental fundamentals of the above-mentioned equations are limited (see, e.g., Refs. [1-5,10-12]). Secondly, there is no
publication on capillary GLC where comparative study of several equations of the type of Eq. (1) has been performed for the experimental data obtained by various research on the various columns coated with different stationary phases under different experimental conditions. Thirdly, quantitative criteria for fitting the data by the equation are not in use in the published studies.

In this paper we perform the comparative study of fitting the experimental data from various research by Eqs. (2), (7) and (11). As noted above, the various physicochemical concepts of band broadening were checked simultaneously.
The correlation coefficient $R$ and Pirson's criterion $\chi^{2}$ [16] were used as the quantitative criteria of the
correlation between the experimental data and Eqs. (2), (7) and (11). Pirson's criterion is usually used for the estimation of the correlation between observed (experimental) and expected (theoretical) data distribution. The lower the $\chi^{2}$ value, the better the correlation observed.

## 2. Experimental

Chromatographic measurements were made on a modified gas chromatograph LKhM-MD (Model 5; 'Khromatograf' Factory, Moscow, Russia) equipped with a flame ionization detection (FID) system.

The characteristics of the systems studied (columns, stationary liquid phases, temperature, carrier gas and compounds chromatographed) are presented in Table 1. Each HETP value was determined as an average of five experiments.

Calculations were performed using standard programme Origin (Version 2.88) for Microsoft Windows.

## 3. Results and discussion

Calculation results are presented in Table 2 and Fig. 1. As can be seen, the Golay equation is preferable for the fitting of the experimental data only in five of 67 considered examples ( $7 \%$ ), the Van

Table 3
Frequency of observed negative values of coefficients of Eqs. (2), (7) and (11))

| Equation | Frequency <br> $(\%)$ | Negative values of the <br> coefficients |
| :--- | :---: | :--- |
| Van Deemter | 100 | Coefficient $A$ in Eq. (11) |
| Golay | 31 | Coefficient $B$ in Eq. (2) |
| Golay-Guiochon | 15 | Coefficient $C$ in Eq. (7) |
|  | 6 | Coefficient $D$ in Eq. (7) |

Deemter equation in 13 (19\%), and the GolayGuiochon equation in 47 cases ( $71 \%$ ). For two considered systems (3\%) the Van Deemter and the Golay equations may fit both the experimental data.
In the present work authors used the results they obtained ( 45 examples, $63 \%$ ) and the literary data ( 26 examples, $37 \%$ ) published.
As follows from the data the Golay-Guiochon equation gives the best fit. Thus, the extra-column band broadening makes a significant contribution into retention since only the Golay-Guiochon equation takes this factor into consideration. Hence, it is expedient to use the Golay-Guiochon equation more widely.
We also estimated the frequency of the observed negative values of the coefficients of Eqs. (2), (7) and (11) when using the same experimental data (see Table 3). It is difficult to get the physicochemical explanation of the phenomenon. As seen from the data listed, the least number of the examples char-


The Golay-Guiochon eq.
Fig. 1. Distribution of the best fit to the various equations.
acterised by negative value of the coefficients observed for the Golay-Guiochon equation.

In our opinion, the results obtained are of interest both for the theory, optimisation of experimental conditions and physicochemical measurements deal with the determination of the values involved in Eq. (7). In our opinion, an analogous equation taking into consideration the extra-column band broadening may be of great importance for liquid chromatography as well.

## 4. Conclusion

The comparative study of three equations (Golay, Golay-Guiochon, and Van Deemter) was originally performed for a great number of experimental data obtained by the authors and found in the scientific literature. It was shown that the Golay-Guiochon equation gives the best fit to the experiment. This justifies that the extra-column contribution is significant since only the Golay-Guiochon equation takes into account this factor.

The Golay-Guiochon equation may be recommended for common use in analytical practice and physicochemical measurements.

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